
Algorithm 7 : Décomposition de Cholesky

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1  $L_{11} \leftarrow \sqrt{a_{11}}$  // 1:√
2 for  $j \leftarrow 2$  to  $n$  do
3   |  $L_{j1} \leftarrow a_{j1}/L_{11}$  //  $(n-1):\otimes$ 
4 end
5 for  $i \leftarrow 2$  to  $n-1$  do
6   |  $L_{ii} \leftarrow \sqrt{a_{ii} - \sum_{k=1}^{i-1} L_{ik}^2}$  //  $(i-2)+1:\oplus\ominus, (i-1):\otimes, 1:\sqrt$ 
7   | for  $j \leftarrow i+1$  to  $n$  do
8     |  $L_{ji} \leftarrow \frac{a_{ji} - \sum_{k=1}^{i-1} a_{jk} L_{ik}}{L_{ii}}$  //  $[n-(i+1)+1]((i-2)+1):\oplus\ominus$ 
9     | //  $[n-(i+1)+1]((i-1)+1):\otimes\otimes$ 
10    | end
11 end
12  $L_{nn} \leftarrow \sqrt{a_{nn} - \sum_{k=1}^{n-1} L_{nk}^2}$  //  $(n-2)+1:\oplus\ominus, (n-1):\otimes, 1:\sqrt$ 
13 return  $L$ ;

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$$N_{\oplus\ominus} = \sum_{i=2}^{n-1} (i-1) + (n-i)(i-1) = \sum_{i=2}^{n-1} (i-1)(1+n-i) = \sum_{i=1}^{n-1} i(n-i) = \frac{n(n^2-1)}{6}.$$